In this talk, I will review a recent application of the S-matrix bootstrap technology to obtain bounds on the two leading Wilson coefficients (or low energy constants) of the chiral lagrangian controlling the low-energy dynamics of massless pions. I will also mention some applications to the gapped QCD case and the possibility of obtaining numerical bounds that relies solely on the rigorously proven analyticity properties of scattering amplitudes