

Monday June 12

10:30 - 12:30

Speaker: David Treumann

Title: Deligne-Lusztig varieties as moduli spaces of sheaves

Abstract: Deligne-Lusztig theory organizes most of the irreducible characters of a finite group G of Lie type of into "series," that are indexed by conjugacy classes of maximal abelian subgroups T of G . The representations in one series are those that appear in the cohomology of an $\overline{\mathbb{F}_p}$ -variety X equipped with an action of the finite group $G \times T$. A basic result of Deligne and Lusztig is "orthogonality", which tells e.g. that representations in the series corresponding to T are different from representations in the series corresponding to T' , when T is not conjugate to T' . It is proved by analyzing a stratification of the quotient $(X \times X')/G$. I will explain how the varieties X and $(X \times X')/G$, and this stratification, arise as moduli spaces of constructible sheaves on a topological annulus. They have something in common with moduli spaces of connections on $\hat{\mathbb{C}}^*$ with irregular singularities at zero and infinity.