

Arpit Dua

***Topological order and error correction on fractal geometries: fractal surface codes***

In this talk, I will focus on topological order, quantum codes, and error correction on fractal geometries. Firstly, I will present a no-go theorem that  $\mathbb{Z}_N$  topological order cannot survive on any fractal embedded in two spatial dimensions and then show that for fractal lattice models embedded in 3D or higher spatial dimensions,  $\mathbb{Z}_N$  topological order survives if the boundaries on the holes condense only loop or membrane excitations. Next, I will discuss fault-tolerant logical gates in the  $\mathbb{Z}_2$  version of these fractal models, which we name fractal surface codes, using their connection to global and higher-form topological symmetries. In the second half of the talk, I will discuss the performance of such fractal surface codes as fault-tolerant quantum memories. I will discuss decoding strategies with provably non-zero thresholds for bit-flip and phase-flip errors in the fractal surface codes with Hausdorff dimension  $2+\epsilon$ . In particular, I will describe the adaptation of the sweep decoder to fractal lattices which maintain its self-correcting and single-shot nature, and state the code performance of a particular fractal surface code with Hausdorff dimension 2.966. I will summarize with ongoing directions.